

## **UNIT 1 GRAPH THEORY**

10 Hrs.

Basic Concepts, Algorithms for connectedness, Shortest path, Minimum Spanning Tree

## **UNIT 2: HIGH DIMENSIONAL SPACE**

10 Hrs.

Properties, Law of large numbers, Sphere and cube in high dimension, Generating points on the surface of a sphere, Gaussians in High dimension, Random projection, Applications.

## **UNIT 3: RANDOM GRAPHS AND SINGULAR VALUE DECOMPOSITION (SVD)**

10 Hrs.

Large graphs,  $G(n, p)$  model, Giant Component, Connectivity, Cycles, Non-Uniform models, Applications. SVD: Best rank  $k$  approximation, Power method for computing the SVD, Applications.

## **UNIT 4: RANDOM WALKS AND ALGORITHM FOR MASSIVE DATA PROBLEMS**

10 Hrs.

Reflection Principle, Long leads, Changes of Sign, Illustrations. Frequency Moments of data streams, matrix algorithms.